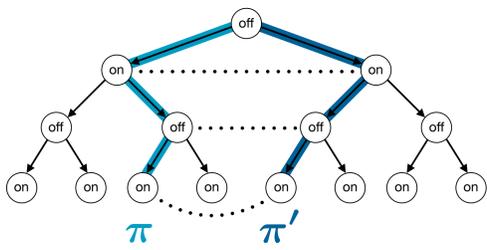


HyperLTL: A Temporal Logic for Hyperproperties

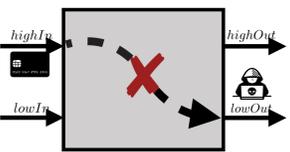
$$\forall \pi. \forall \pi'. \square (on_{\pi} \leftrightarrow on_{\pi'})$$



$$\varphi := \forall \pi. \varphi \mid \exists \pi. \varphi \mid \psi$$

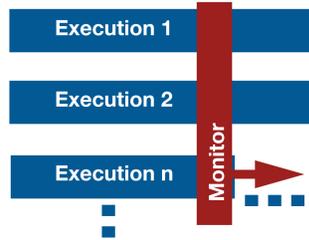
$$\psi := a_{\pi} \mid \psi \wedge \psi \mid \neg \psi \mid \bigcirc \psi \mid \psi \mathcal{U} \psi$$

- HyperLTL handles relations between traces (hyperproperties) by explicit quantification
- Can express information-flow policies, symmetry, Hamming-distance and alike.
- For example, noninterference:



$$\forall \pi. \forall \pi'. (o_{\pi} = o_{\pi'}) \mathcal{W}(i_{\pi} \neq i_{\pi'})$$

Challenges in Monitoring Hyperproperties



- Previously seen executions have to be stored to determine the satisfaction of a hyperproperty
- Algorithmic workload increases with the number of incoming traces
- Our model: monitor observes incoming traces sequentially

Optimizations in Monitoring Hyperproperties

Trace Analysis:

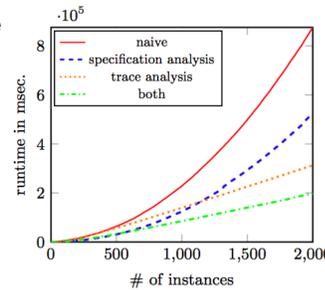
- Prunes redundant execution traces that pose strictly less requirements on future traces than others
- Small overhead, because an on the fly implementation

→ Keeps the minimal set of traces needed to provide a counter example at the earliest possible point in time

Specification Analysis:

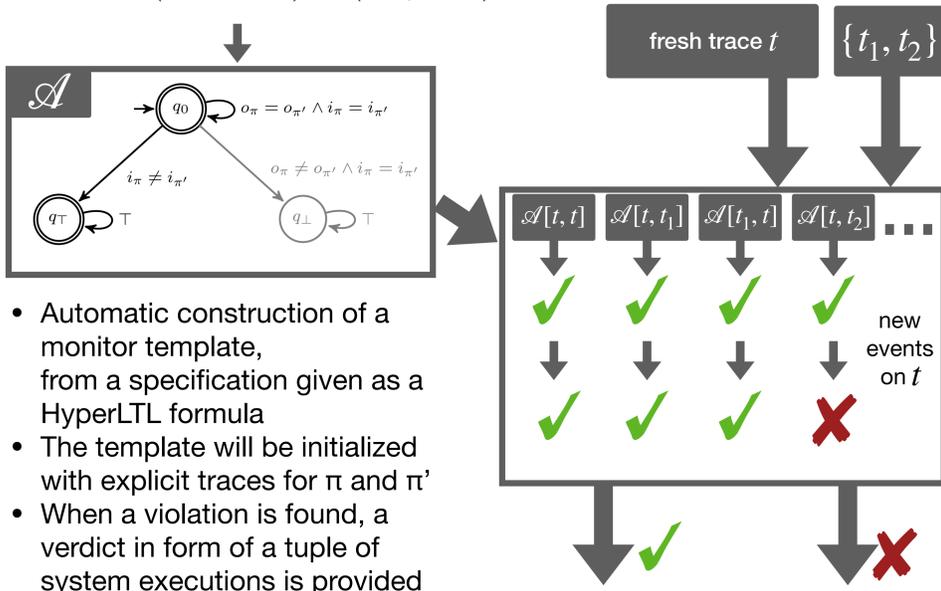
- Reduces the number of comparisons between incoming traces by analyzing the HyperLTL formula
- The HyperLTL SAT solver EAHyper is used to detect whether a formula is reflexive, symmetric or transitive

→ Reduces the algorithmic workload needed to detect a violation



Automaton-based Monitoring Approach

$$\forall \pi. \forall \pi'. (o_{\pi} = o_{\pi'}) \mathcal{W}(i_{\pi} \neq i_{\pi'})$$



- Automatic construction of a monitor template, from a specification given as a HyperLTL formula
- The template will be initialized with explicit traces for π and π'
- When a violation is found, a verdict in form of a tuple of system executions is provided

→ Despite the optimization efforts, at least quadratic in the number of incoming traces

no violation: add t to $\{t_1, t_2\}$ and proceed

violation: report counter example

Constraint-based Monitoring Approach

$$\forall \pi, \pi'. (out_{\pi} \leftrightarrow out_{\pi'}) \mathcal{W}(in_{\pi} \leftrightarrow in_{\pi'})$$

$$(in_{\pi} \leftrightarrow in_{\pi'}) \vee (out_{\pi} \leftrightarrow out_{\pi'}) \wedge \bigcirc ((out_{\pi} \leftrightarrow out_{\pi'}) \mathcal{W}(in_{\pi} \leftrightarrow in_{\pi'}))$$

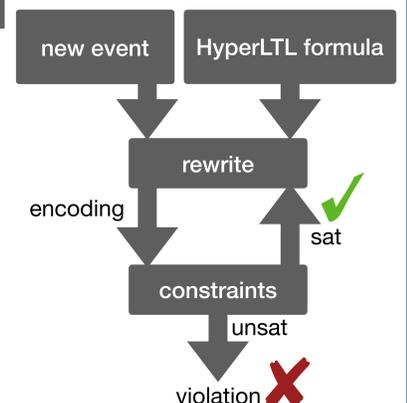
event {in, out}

$$(\top \leftrightarrow in) \vee (\top \leftrightarrow out) \wedge \bigcirc ((out_{\pi} \leftrightarrow out_{\pi'}) \mathcal{W}(in_{\pi} \leftrightarrow in_{\pi'}))$$

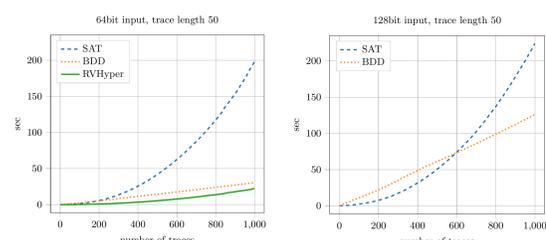
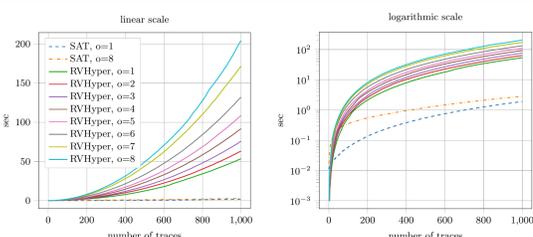
$$\neg in \vee out \wedge \bigcirc ((out_{\pi} \leftrightarrow out_{\pi'}) \mathcal{W}(in_{\pi} \leftrightarrow in_{\pi'}))$$

- Algorithm rewrites a HyperLTL formula and single event into a constraint composed of an LTL part and a HyperLTL part
- Incrementally build a constraint system by encoding the HyperLTL part as a variable

→ Solely store necessary information (instead of entire traces) to detect violations of a hyperproperty



Experimental Results: Comparing the two Approaches



- Guarded invariants (top)

$$\forall \pi, \pi'. \diamond (\vee_{i \in I} i_{\pi} \leftrightarrow i_{\pi'}) \rightarrow \square (P(\pi) \leftrightarrow P(\pi'))$$
- Noninterference (bottom)

$$\forall \pi, \pi'. (o_{\pi} = o_{\pi'}) \mathcal{W}(i_{\pi} \neq i_{\pi'})$$
- Dependencies between input and output signals in hardware designs (table)

$$\forall \pi_1 \forall \pi_2. (o_{\pi_1} \leftrightarrow o_{\pi_2}) \mathcal{W}(i_{\pi_1} \leftrightarrow i_{\pi_2})$$

instance	# traces	length	time RVHyper	time SAT	time BDD
XOR1	19	5	12ms	47ms	49ms
XOR2	1000	5	16913ms	996ms	1666ms
counter1	961	20	9610ms	8274ms	303ms
counter2	1353	20	19041ms	13772ms	437ms
MUX1	1000	5	14924ms	693ms	647ms
MUX2	80	5	121ms	79ms	81ms

Implementation

- Two approaches for monitoring hyperproperties: automaton-based and constraint-based
- Constraint-based approach ensures more fine grained storage handling
- SAT implementation especially suited for guarded invariants
- Source code + Benchmarks are available: <https://www.react.uni-saarland.de/tools/>



→ A complete tool box for the efficient runtime verification of hyperproperties in reactive systems