Prof. Bernd Finkbeiner, Ph.D. Martin Zimmermann, Ph.D. Leander Tentrup, B.Sc. Summer term 2013 Problem Set 17 October 1, 2013

Verification

Problem 1: Cooper's Method [8 Points]

Apply quantifier-elimination to the following $\Sigma_{\mathbb{Z}}$ -formulae.

- a) $\forall y. \ 3 < x + 2y \lor 2x + y < 3$
- b) $\exists y. \ 3 < x + 2y \lor 2x + y < 3$

The following exercises belong to the afternoon session.

Problem 2: Congruence Closure Algorithm [8 Points]

Apply the decision procedure for T_E to the following Σ_E formulae:

a)
$$f(f(f(a))) = f(a) \wedge f(f(a)) = a \wedge f(a) \neq a$$

b)
$$f(f(f(a))) = f(f(a)) \wedge f(f(f(f(a)))) = a \wedge f(a) \neq a$$

- c) $f(g(x)) = g(f(x)) \wedge f(g(f(y))) = x \wedge f(y) = x \wedge g(f(x)) \neq x$
- d) $p(x) \wedge f(f(x)) = x \wedge f(f(f(x))) = x \wedge \neg p(f(x))$