## Embedded Systems

Please indicate your name, group number, and discussion slot tutor. Only one submission per group is necessary.

## Problem 1: A/D Conversion

In the lecture we discussed the successive approximations method as one possibility for converting analog signals into digital values. Using the successive approximations method, carry out the conversion of the input voltages $U_{\text {in }}=2.8 \mathrm{~V}, 1.6 \mathrm{~V}$, and 3.55 V into the corresponding binary values. In each case, give the final binary value, and for each step of the conversion, show:

1. the arranged comparison voltage $U_{\text {ref }}$;
2. the binary value for each comparison.

The digital value should have a precision of 4 bits. Assume also that the working range of the A/D converter lies between $U_{\min }=1 V\left(0000_{2}\right)$ and $U_{\max }=4 V\left(1111_{2}\right)$.

## Problem 2: SIMD

Assume that we have a single-instruction multiple-data (SIMD) processor with a 64 -bit input port and a 64-bit output port. The processor does not have any external memory other than the 64 -bit registers mm 0 to mm 7 , and the following instructions, where $x$ and $y$ refer to any register, and $z$ can refer to (the value of) any register or any constant:

| Command | Explanation |
| :--- | :--- |
| read x | Obtains a new 64-bit value from the input port and stores it to <br> register $x$. Blocks until 64 bits of data are available. |
| write x | Writes $x$ to the output port. Blocks until data can be written. |
| jump j | Jumps to label $j$ in the program |
| and $\mathrm{x}, \mathrm{y}, \mathrm{z}$ | Takes a bit-wise AND of $z$ and the value in register $y$, and stores <br> it to register $x$ |
| or $\mathrm{x}, \mathrm{y}, \mathrm{z}$ | Takes a bit-wise OR of $z$ and the value in register $y$, and stores it <br> to register $x$ |
| shift $\mathrm{x}, \mathrm{y}, \mathrm{c}$ | Shifts the content of register $y$ by $c$ (which is a constant between <br> -64 and 64 ), and stores the result into register $x$. Fills with 0s. |
| paddw $\mathrm{x}, \mathrm{y}, \mathrm{z}$ | A SIMD instruction: Divides $y$ and $z$ into 16 -bit wide words (repre- <br> senting unsigned integer values), adds the $i$ th chunk of $y$ to the $i$ th <br> chunk of $z$ for every $i \in\{1,2,3,4\}$, and stores the results together <br> in register $x$ |
| pmullw $\mathrm{x}, \mathrm{y}, \mathrm{z}$ | A SIMD instruction: Divides $y$ and $z$ into 16 -bit wide words (repre- <br> senting unsigned integer values), multiplies the $i$ th chunk of $y$ with <br> the $i$ th chunk of $z$ for every $i \in\{1,2,3,4\}$, and stores the results <br> together in register $x$ |

Assume that the processor gets a data stream $\vec{X}=X_{0} X_{1} X_{2} \ldots$ of 16-bit words fed to its input port such that every reading operation reads four values at once. Create a program to let the processor output a stream of 16 -bit integers $\vec{Y}=Y_{0} Y_{1} Y_{2} \ldots$ such that for every $i \in \mathbb{N}$, we have $Y_{i}=\left(X_{i}+X_{i+1}+3\right) \cdot 2$. You can use labels in your program as targets for the jump operation. After reading some values, the output does not have to be produced immediately, but outputting may be delayed. Note that the write operation will also output four items of the $Y$ stream at once. You can use binary or hexadecimal notation for all constants if you wish. We assume that for all $i \in \mathbb{N}$, we have $0 \leq X_{i}<16000$, and the addition and multiplication operations will behave in some bad non-specified way upon overflows. All arithmetic operations work on non-negative numbers.

## Problem 3: Aperiodic Scheduling

Assume a uniprocessor architecture without preemption. Consider the following set of asynchronous, aperiodic, and independent tasks:

| Job | $J_{1}$ | $J_{2}$ | $J_{3}$ | $J_{4}$ |
| :--- | :---: | :---: | :---: | :---: |
| Arrival time $a$ | 0 | 4 | 2 | 6 |
| Computation time $C$ | 6 | 2 | 4 | 2 |
| Deadline $d$ | 16 | 10 | 9 | 12 |

Is the given task set schedulable? If it is, your task is to find the schedule.

