

# Symbolic vs. Bounded Synthesis for Petri Games

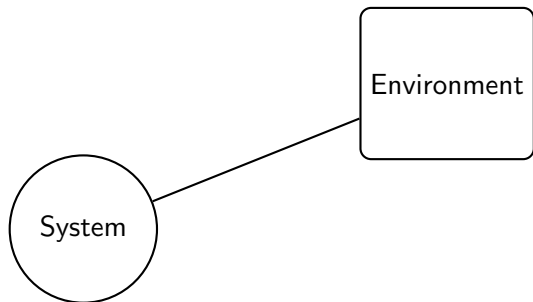
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Jesko Hecking-Harbusch<sup>1</sup>, Ernst-Rüdiger Olderog<sup>2</sup>

<sup>1</sup>Universität des Saarlandes

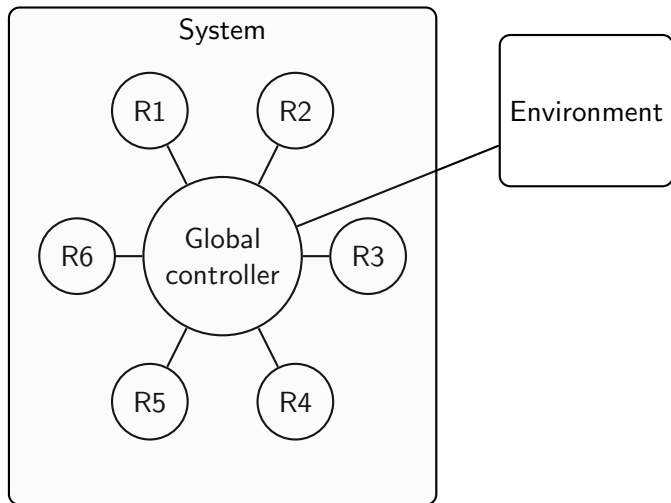
<sup>2</sup>Carl von Ossietzky Universität Oldenburg

SYNT, July 22, 2017

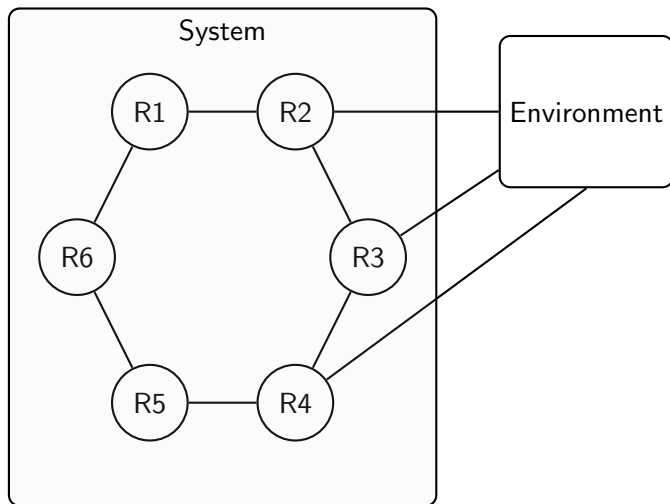
# Synthesis



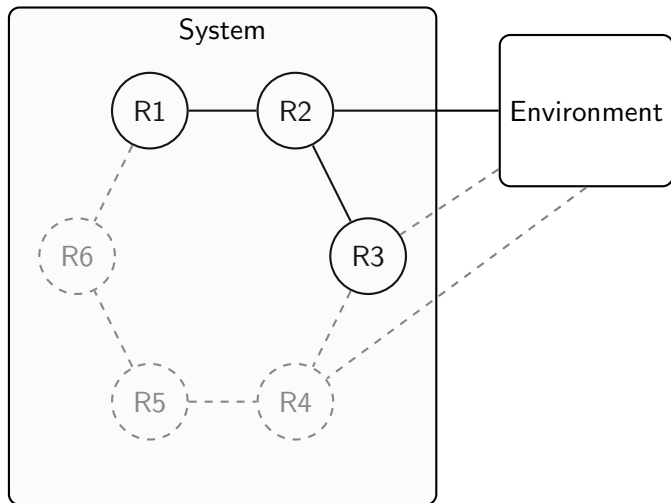
# Synthesis



# Distributed Synthesis



## Local Information



# Distributed Synthesis with Petri Games

[Finkbeiner, Olderog, '14]

Existing tool:

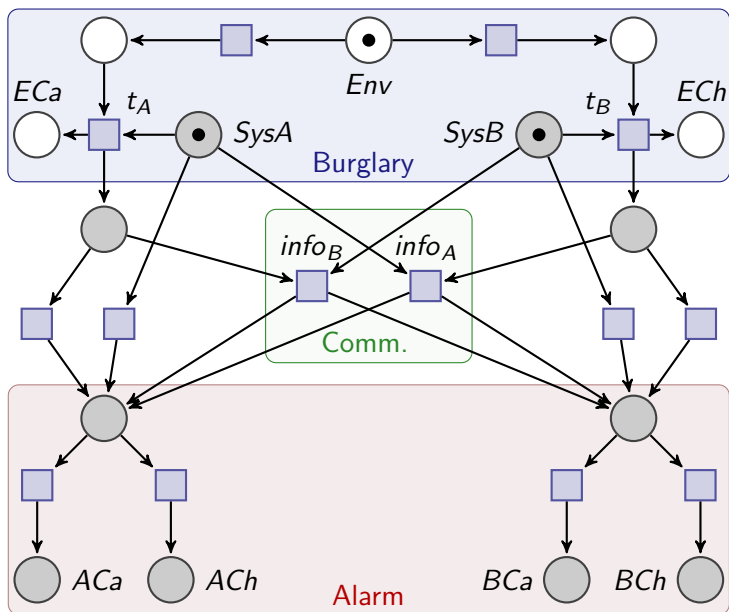
- ▶ ADAM is used to synthesize Petri games *symbolically*.

New tool:

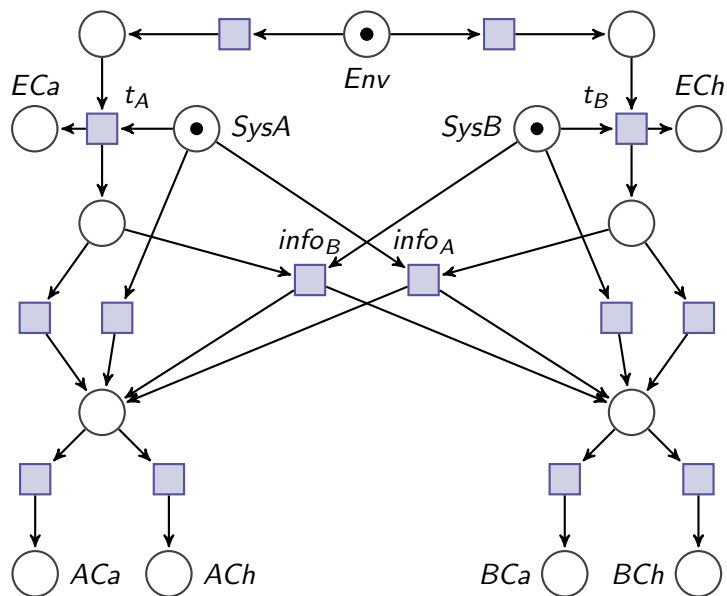
- ▶ Prototype implementation of *bounded synthesis*.

We compare experimental results of the two approaches.

# Distributed Alarm Systems

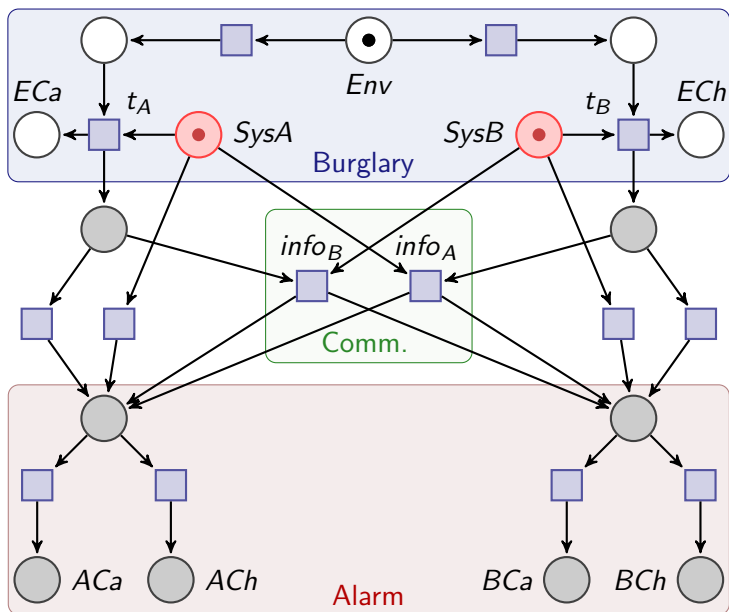


## Petri Games are based on Petri Nets

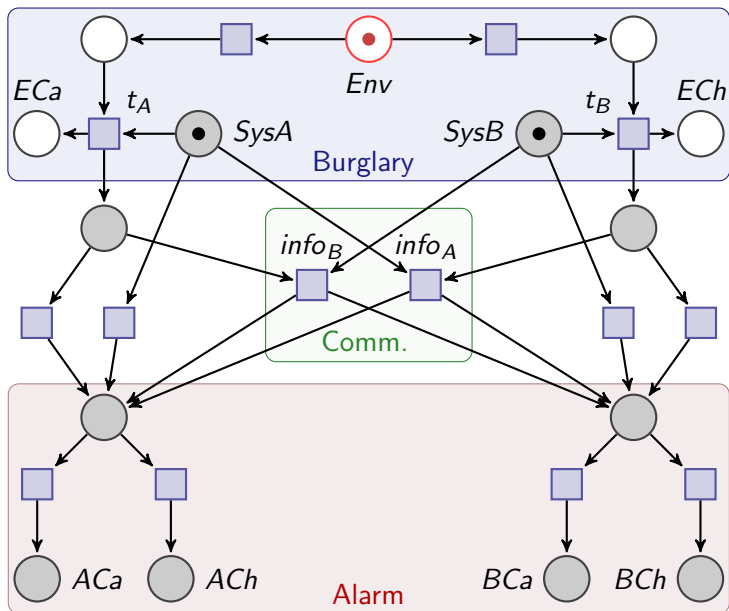




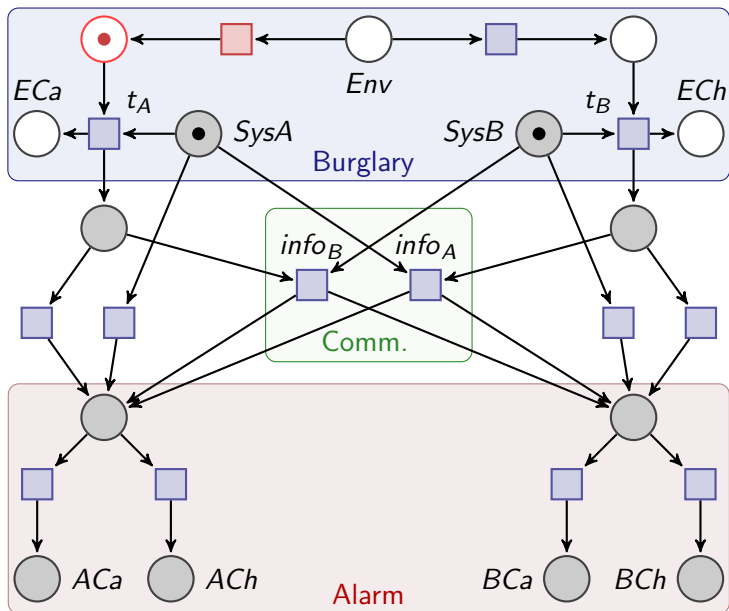
## Two System Players



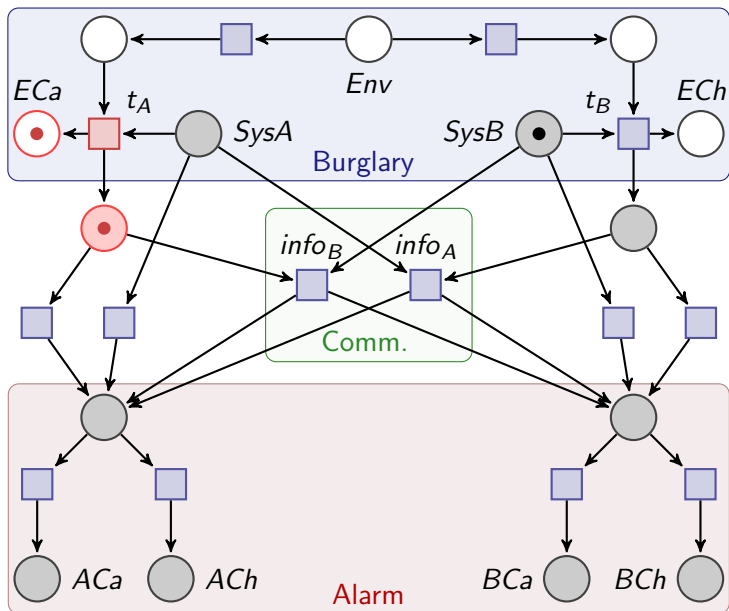
# One Environment Player



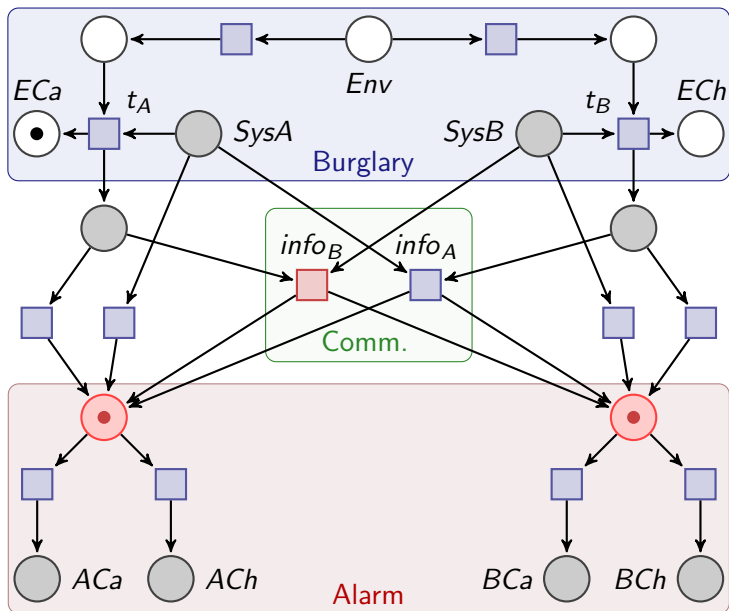
# Intrusion at Location A



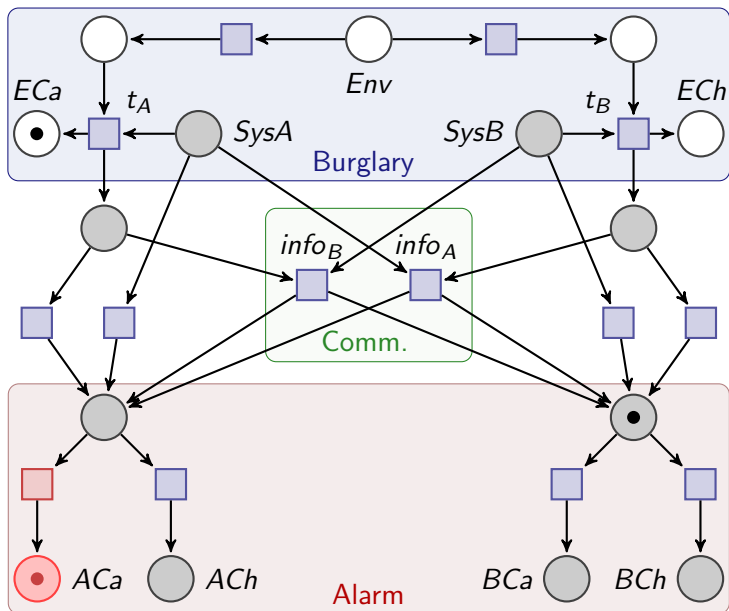
# Detection of Intrusion via Synchronization



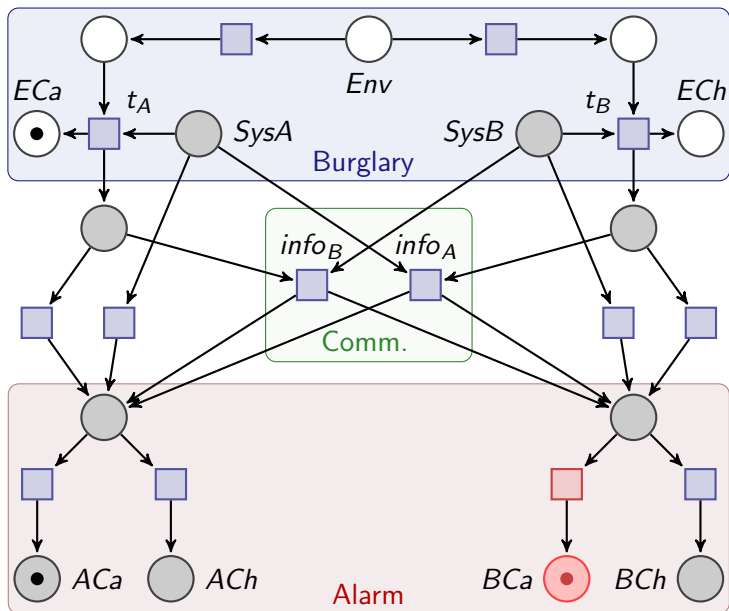
# Exchange of Information via Synchronization



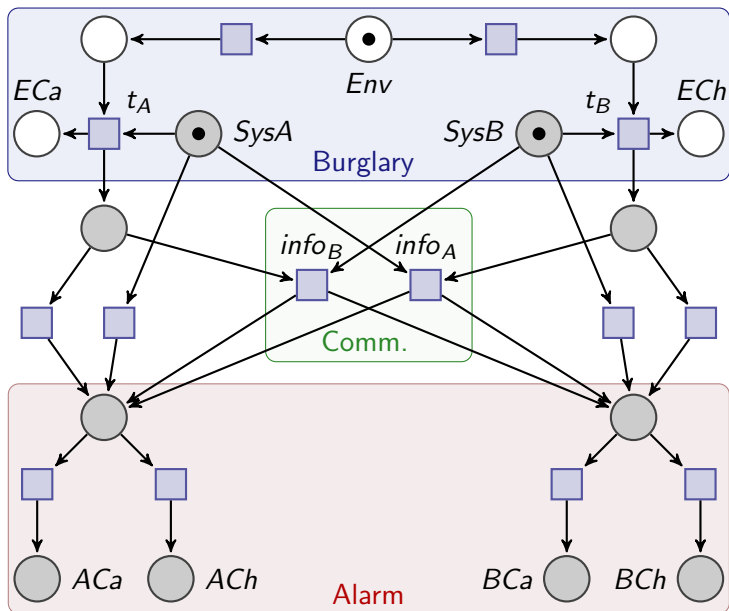
# Setting-Off an Alarm



## Setting-Off the Second Alarm

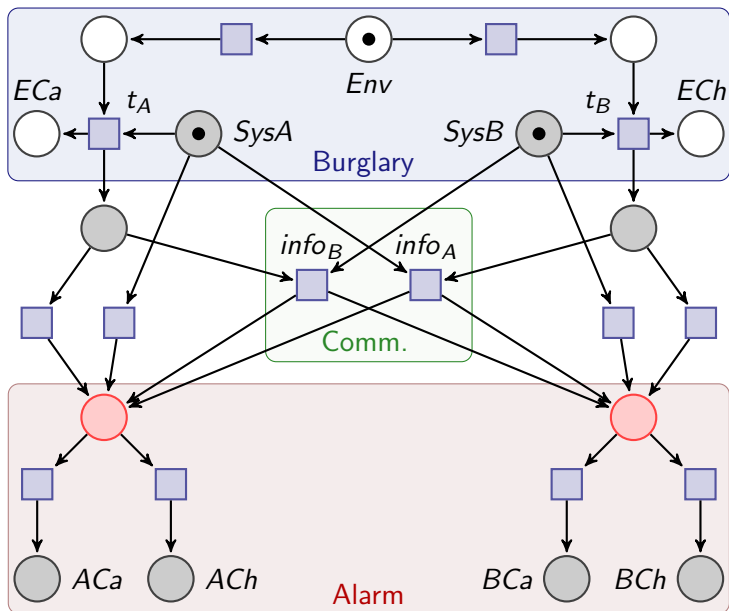


## System Players can Refuse to Fire Transitions...

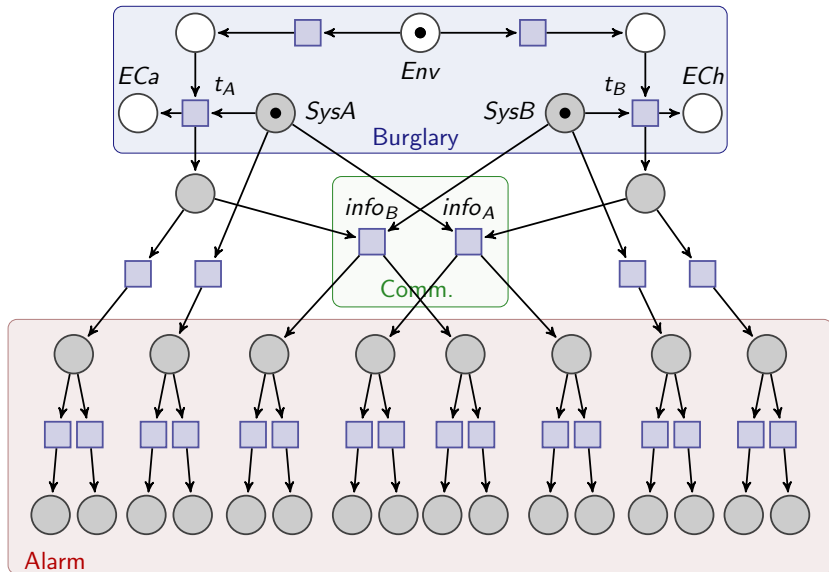




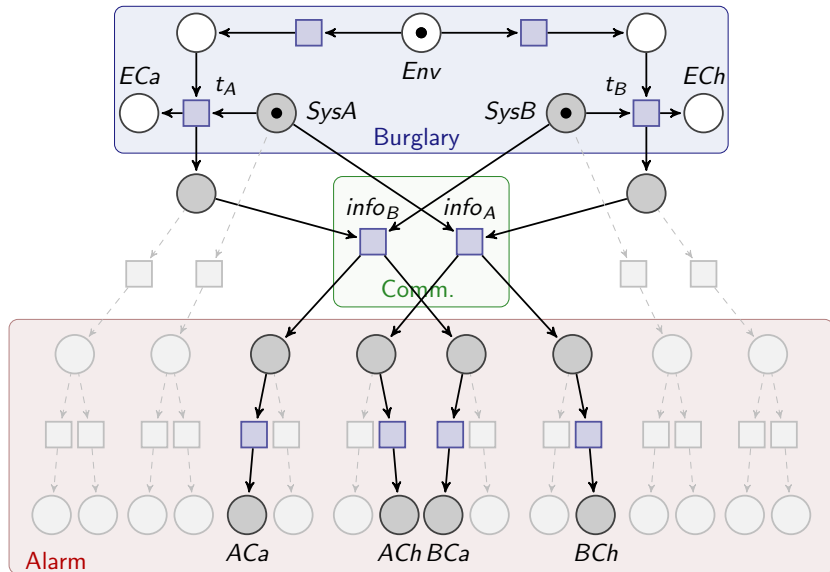
...Based on their Causal Memory



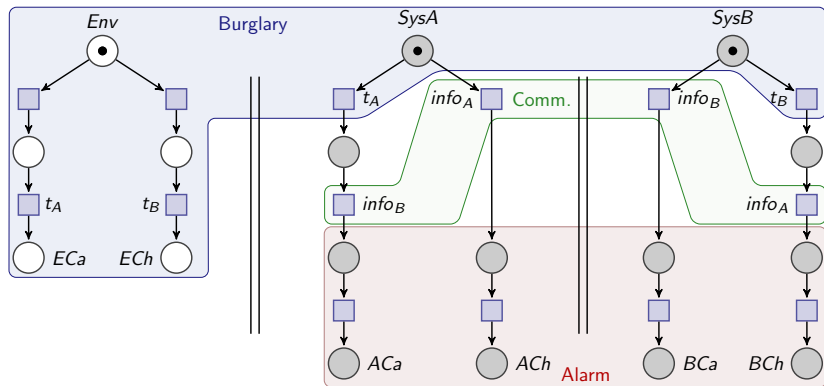
# Unfolding of Distributed Alarm System



# Winning Strategy of Distributed Alarm System



# Local controllers for Distributed Alarm System



# Complexity of Solving Petri Games

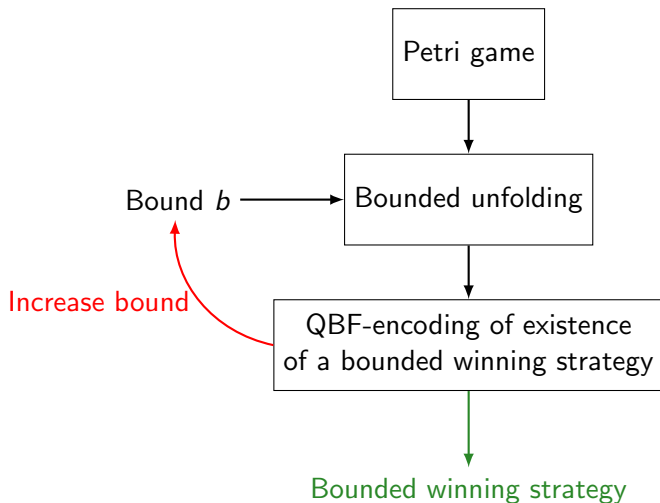
For a single environment token and a bounded number of system tokens, deciding the existence of a safety strategy for the system players is EXPTIME-complete [Finkbeiner, Olderog, '14].

# Complexity of Solving Petri Games

For a single environment token and a bounded number of system tokens, deciding the existence of a safety strategy for the system players is EXPTIME-complete [Finkbeiner, Olderog, '14].

Underlying reduction to a Büchi game implemented in ADAM symbolically [Finkbeiner, Giesekeing, Olderog, '15].

# Bounded Synthesis for Petri Games



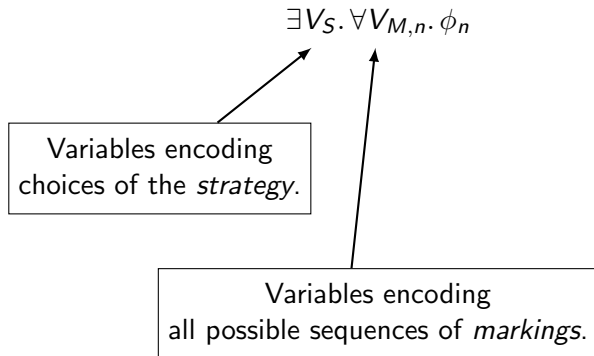
# QBF-Encoding of Existence of Bounded Winning Strategy

$$\exists V_S. \forall V_{M,n}. \phi_n$$

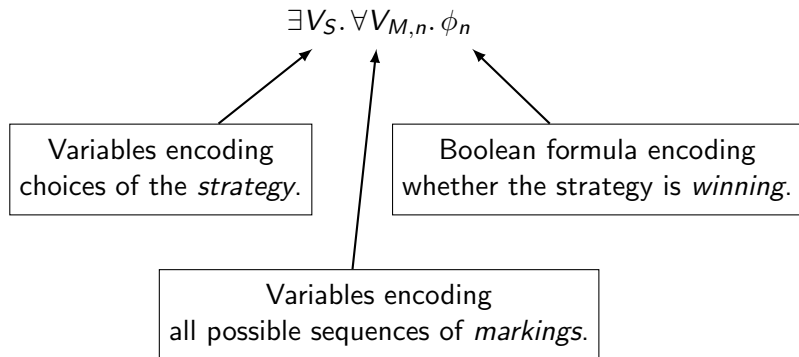
Variables encoding  
choices of the *strategy*.



# QBF-Encoding of Existence of Bounded Winning Strategy

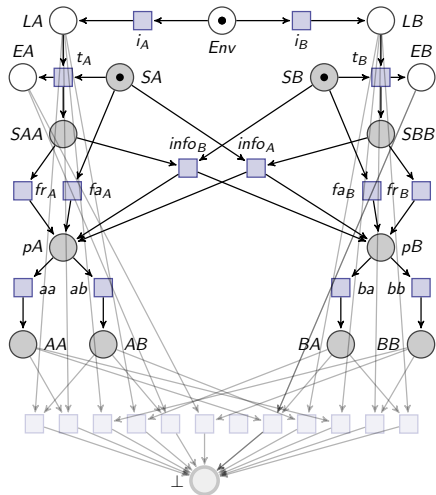


# QBF-Encoding of Existence of Bounded Winning Strategy

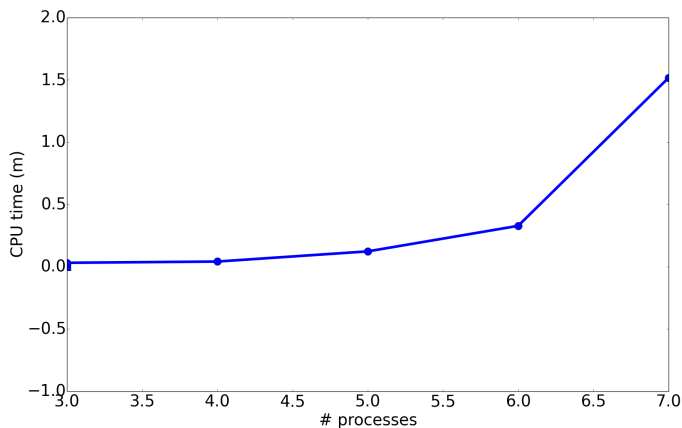


# Benchmark – Distributed Alarm System

- ▶ The environment can intrude one of  $n$  locations.
- ▶ All  $n$  locations have to indicate where the intrusion occurred.
- ▶ Scalable in  $n$



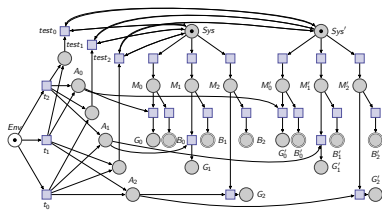
# Runtime – Distributed Alarm System



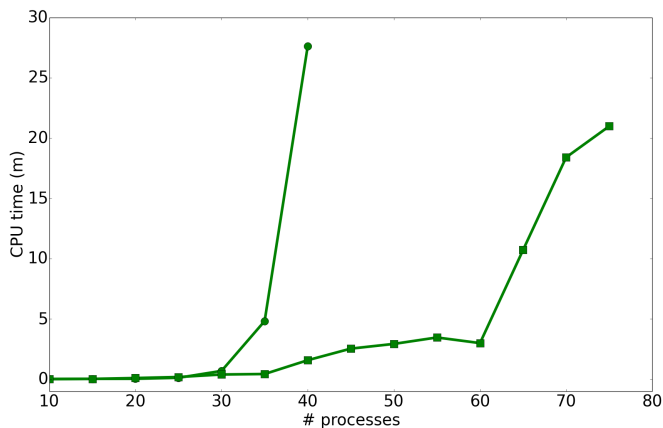
- winning strategy of symbolic approach,
- winning strategy of bounded approach

# Benchmark – Concurrent Machines

- ▶  $k$  orders to manufacture goods are processed by  $n$  distributed machines.
- ▶ The environment can destroy one machine.
- ▶ The orders have to avoid the defective machines and each machine can process at most one order.
- ▶ Scalable in  $n$  and  $k$



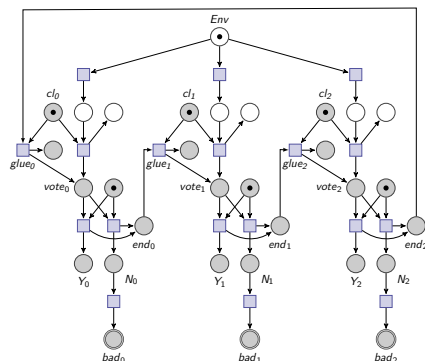
# Runtime – Concurrent Machines



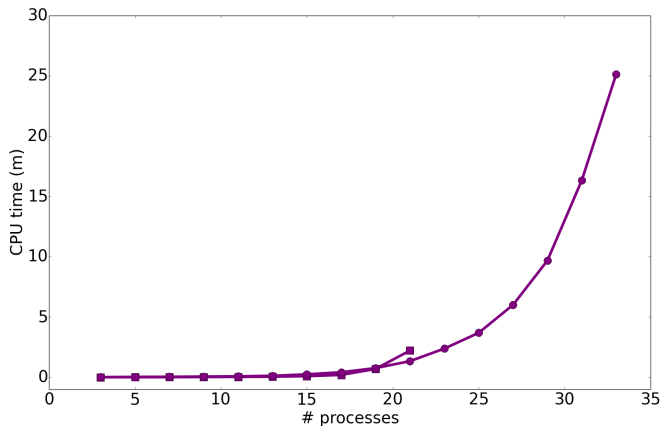
- winning strategy of symbolic approach,
- winning strategy of bounded approach

# Benchmark – Document Workflow simple

- ▶  $n$  clerks should endorse a document.
- ▶ The environment decides which clerk gets the document first.
- ▶ scalable in  $n$



## Runtime – Document Workflow simple

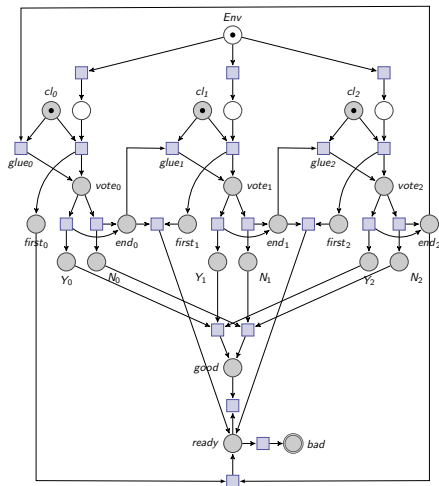


- winning strategy of symbolic approach,
- winning strategy of bounded approach

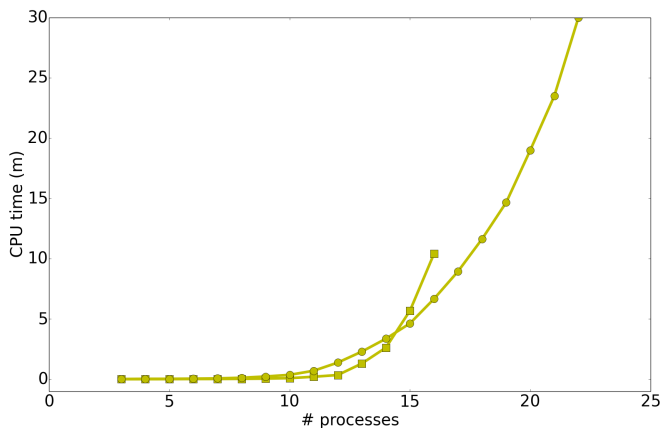


# Benchmark – Document Workflow

- ▶  $n$  clerks have to make a unanimous decision to endorse or reject the document.
- ▶ The environment decides which clerk has to start.
- ▶ scalable in  $n$



# Runtime – Document Workflow

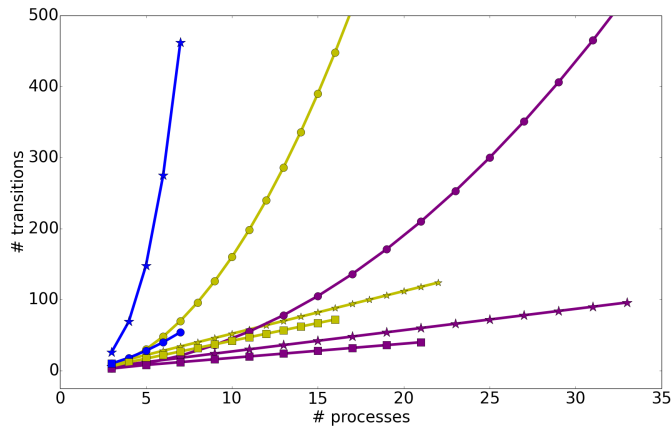


- winning strategy of symbolic approach,
- winning strategy of bounded approach

# Results for Comparison of Runtime

- ▶ The symbolic approach has better runtime for benchmarks with numerous transitions to bad places.
- ▶ The bounded approach synthesizes distributed systems with up to 75 processes.

# Strategy Size of Symbolic and Bounded Approach



- ★ input Petri game
- winning strategy of symbolic approach
- bounded winning strategy

## Results for Comparison of Strategy Size

- ▶ The bounded unfolding allows succinct representation of situations where the same decision suffices for different causal pasts.

# Conclusions

- ▶ Petri games are the first scalable framework for distributed synthesis of systems with up to 75 distributed components.
- ▶ Winning strategies of the bounded approach are by order of magnitude smaller than winning strategies of the symbolic approach.
- ▶ Bounded synthesis solves games with more than one environment player which we plan to realize for the symbolic approach in future work (including further benchmarks).